

# Forest Carbon Sequestration under uncertainty

## When Not in the Best of Worlds

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# Introduction

# Background and Question

- Climate change
- Forest carbon sequestration, a low cost abatement strategy
- Uncertainties concerning sequestration potential
- How does uncertainty affect forest carbon sequestration?
- Our contribution

# Model

- Integrated assessment model: DICE2007 (Nordhaus)
- Economic growth model with a climate damage function
- Maximizes the present value of the social welfare function
- Two control variables: investment and carbon control rate (the transition from carbon to non-carbon energy)
- FOR-DICE (Eriksson 2015) with global forest biomass, bioenergy harvest, avoided deforestation
- Extended to include afforestation, climate feedback on forest
- Three types of forest sequestration control variables: avoided deforestation, afforestation, bioenergy harvest

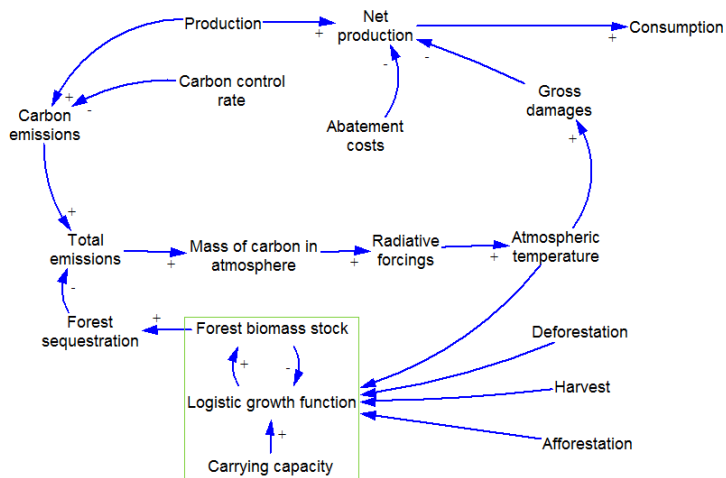
# Uncertainty

How uncertainty is modeled will affect the robustness of the results and policy implications

- Truly stochastic  
Decision in each period made prior to realization
- Averaging multiple runs  
All uncertainty resolved before optimization
- Contingent state  
Uncertainty as multiple states of the world, partly resolved before optimization  
Random parameters drawn from distributions in advance

# The Model

# The Big Picture



# Forest Dynamics (tropical, boreal, temperate)

Logistic growth for stocks of biomass

$$F_{n,t+1} = F_{n,t} + \psi_{n,t} F_{n,t} \left[ 1 - \frac{F_{n,t}}{F_{n,t}^{MAX}} \right] - H_{n,t} - D_{n,t} - B_{n,t}, \quad (1)$$

$n$  is type of forest,  $F_{n,t}$  is stock of forest biomass,  $\psi_{n,t}$  is growth rate,  $H_{n,t}$  is total harvest.  $D_{n,t}$  is loss from deforestation,  $B_{n,t}$  is loss from climate change

Carrying capacity

$$F_{n,t+1}^{MAX} = F_{n,t}^{MAX} - \frac{F_{n,t}^{MAX}}{F_{n,t}} D_{n,t} + A_{n,t} + G_{n,t}. \quad (2)$$

$\frac{F_{n,t}^{MAX}}{F_{n,t}}$  is a rescaling factor,  $A_{n,t}$  is afforestation increase,  $G_{n,t}$  is climate induced change



# Climate feedback on forest

An increased global mean temperature affects forest

Intrinsic growth rate

Degree	Tropical	Boreal	Temperate
2	-6.8%	9.3%	-5.1%
3	-21%	-26%	-16%

Geographical distribution (affects carrying capacity in model)

Degree	Tropical	Boreal	Temperate
2	-1.6%	2.9%	-
3	-5.0%	9.0%	-

# Forest Control Variables

- **Avoided deforestation (tropical)**  
Opportunity cost - rental payment to prevent conversion of forest land  
Marginal cost function derived from Kinderman et al (2008)  
cost
- **Afforestation (tropical, temperate)**  
Opportunity cost + plantation cost  
Marginal cost function estimated from GAEZ v3 crop production/hectare  
cost
- **Bioenergy harvest (tropical, temperate, boreal)**  
Bioenergy harvest contributes to energy by a nested Cobb-Douglas function calibrated with data from IEA and FAO  
No extraction cost

# Energy

Total energy used in production = fossil energy ( $FO_t$ ) + forest bioenergy ( $HB_{n,t}$ ) + non-carbon energy ( $\mu_t$ )

Carbon emissions:

$$\Pi_t = Y_t \sigma_t (1 - \mu_t) \quad (3)$$

$Y_t$  is gross production,  $\sigma_t$  is ratio of uncontrolled emission to output,  $\mu_t$  is carbon control rate (mitigation)

Carbon energy required:

$$\Xi_t = \Pi_t \xi \quad (4)$$

$\xi_t$  is energy emission parameter

Carbon energy sources:

$$\Xi_t = \varsigma HB_{tro,t}^{\beta_{tro}} HB_{bor,t}^{\beta_{bor}} HB_{tem,t}^{\beta_{tem}} FO_t^{1-(\beta_{tro}+\beta_{bor}+\beta_{tem})} \quad (5)$$

# Emissions

Total carbon emissions = emission from energy ( $E_t$ ) - forest sequestration ( $EF_t$ )

Emission from energy:

$$E_t = FO_t + \sum_n HB_{n,t} \theta_n \quad (6)$$

$FO_t$  is fossil energy,  $HB_{n,t}$  is bionergy harvest,  $\theta_n$  is conversion factor

Carbon sequestration:

$$EF_{n,t} = (F_{n,t} - F_{n,t-1}) \theta_n \quad (7)$$

$F_{n,t}$  is stock of forest biomass

# Output

Final output:

$$Q_t = \frac{1}{(1 + \pi_1 \Delta T_t^{\pi_2})} (1 - \Lambda_t) Y_t - CD_t - \sum_n CA_{n,t} \quad (8)$$

$\Delta T_t$  is temperature increase,  $\Lambda_t$  is carbon control cost,  $CD_t$  is cost of avoiding deforestation,  $CA_{n,t}$  is cost of afforestation

Per capita consumption:

$$c_t = \frac{Q_t - I_t}{L_t} \quad (9)$$

Utility function:

$$U_t(\cdot) = L_t \left( \frac{c_t^{1-\alpha}}{1-\alpha} \right) \quad (10)$$

$L_t$  is population/labor,  $\alpha$  is elasticity of the marginal utility of consumption

# Uncertainty

Contingent state optimization:

$$W = \max_{I_t, \mu_t, RD_{n,t}, HA_{n,t}, HB_{n,t}} \frac{1}{S} \sum_{s=1}^S \sum_{t=1}^T (1 + \rho)^{-t} U_{s,t}(\cdot) \quad (11)$$

$s$  is state index,  $I_t$  is investment,  $\mu_t$  is carbon control rate,  $RD_{n,t}$  is reduction of deforestation,  $HA_{n,t}$  is afforestation,  $HB_{n,t}$  is harvest bioenergy,  $\rho$  is pure rate of time preference

Uncertainty parameters

	tropical	boreal	temperate
Initial intrinsic growth	N(0.199, 0.04)	N(0.373, 0.04)	N(0.113, 0.04)
Climate feedback on intrinsic growth	N(-0.04, 0.02)	N(-0.03, 0.015)	N(-0.79, 0.027)
Climate feedback on forest cover change	N(-20,10)	N(0.2)	N(20,10)

# Preliminary Results

# Recognizing uncertainty

Comparing without and with forest control. Metric: carbon price

## No uncertainty

Carbon price	2015	2035	2055	2075
Carbon control	41.6	81.2	137.8	215.7
All controls	41.5	81.0	137.6	216.0

⇒ small difference between with or without forest control

## Forest uncertainty

Carbon price	2015	2035	2055	2075
Carbon control	62.5	153.9	355.2	736.3
All controls	41.5	81.1	138.0	217.0

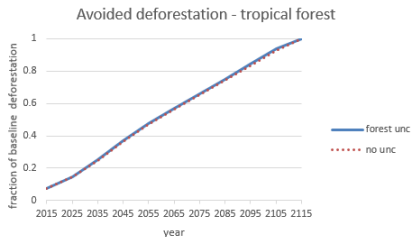
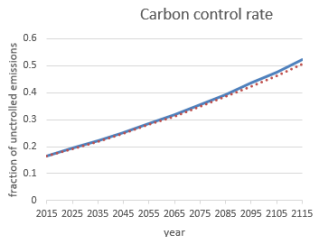
⇒ large difference between with or without forest control

Carbon control is not enough when forest uncertainty is introduced.



# Rebalancing of controls 1

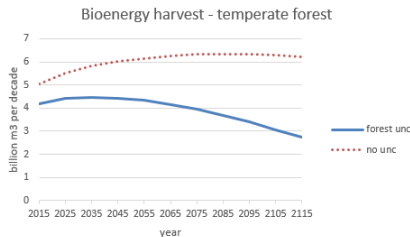
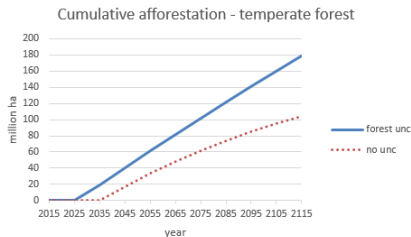
Comparing with and without uncertainty when using all controls.  
Metric: carbon control rate and avoided deforestation



⇒ A small difference

# Rebalancing of controls 2

Comparing with and without uncertainty when using all controls.  
Metric: optimal cumulative afforestation and optimal bioenergy harvest.



⇒ A big difference

Forest uncertainty makes a rebalancing of controls necessary.

# More insights

- Better to reduce bioenergy (short-term) harvest than to increase afforestation (long-term)
- The forest type with the least uncertainty regarding growth rate is preferred when rebalancing
- The balance between forest and carbon control is clearly affected by uncertainty
- Ignoring uncertainty will give a biased estimate of costs and hence the wrong carbon price.

# Thank you

# Thank you!

# Deforestation Marginal Cost

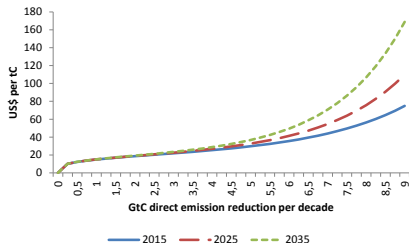


Figure : Cost of avoiding emissions from deforestation

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# Afforestation Marginal Cost

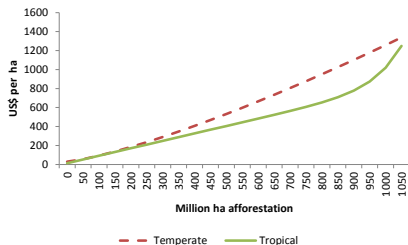


Figure : Cost of afforestation

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